

# The efficiency consequences of local revenue equalization: Tax competition and tax distortions\*

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24 July 2002

## Abstract

This paper shows how a popular system of federal revenue equalization grants can limit tax competition among subnational governments, correct fiscal externalities, and increase government spending. Remarkably, an equalization grant can implement efficient policy choices by regional governments, regardless of a wide variety of differences in regional tax capacity, tastes for public spending, and population. If aggregate tax bases are elastic, however, equalization leads to excessive taxation. Efficiency can be achieved by a modified formula that equalizes a fraction of local revenue deficiencies equal to the fraction of taxes that are shifted backward to factor suppliers.

**JEL code:** H7

**Keywords:** tax competition, intergovernmental grants

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\*Thanks to Robin Boadway, Jean Hindriks, Mats Persson, Torsten Persson, and other seminar participants for comments.

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# 1 Introduction

Decentralization of spending powers to lower-level governments is a widespread phenomenon, one which appears to have become more common in recent years. The benefits of decentralization are familiar to economists, at least since the work of Tiebout (1956). Decentralization has often been held to increase the responsiveness of policy to the preferences of citizens, and to increase accountability in government. Some of the costs of decentralization are also familiar.<sup>1</sup> If government spending must be financed from local fiscal resources, then it is apt to be distributed unequally among regions. But decentralization is known to have potentially negative consequences for efficiency as well as equity. When tax bases are mobile among regions in a federation, then uncoordinated local policy-making may exert downward pressure on government spending everywhere, distorting the mix of public and private consumption. Further, unharmonized local policies can distort the allocation of mobile resources among regions, which leads to failures of production efficiency. These and a variety of other fiscal spillovers among regions can make outcomes Pareto inefficient in a decentralized federation.

A variety of reforms have been proposed to correct these different problems associated with decentralization. In this paper, we argue that one simple mechanism available to federal governments—equalization grants—can in a wide variety of circumstances address both the efficiency and equity problems of decentralization.

An equalization grant is a particular system of federal revenue sharing that is already employed in a number of countries.<sup>2</sup> In its idealized form, an equalization system sets the (per capita) transfer to each government equal to the difference between its tax capacity and the average capacity of all regions, multiplied by some “standard” tax rate, usually equal to the average of all regions’ tax rates. Tax capacity is measured in turn by the observed per capita tax base of each jurisdiction. Thus the program aims to equalize differences in tax revenue, but implements transfers through an indirect formula, based on differences in observed tax bases.

That equalization can make the regional distribution of public goods more equitable should be clear. Indeed, when all governments choose the same tax rate, the formula guarantees equal per capita net revenues. The impact of the formula on efficiency of tax policies in a world of mobile tax bases is more subtle, but still straightforward. A tax cut by a single region causes an inflow of the tax base to the region, which mitigates the revenue loss of the tax cut, but at the expense of government revenues in other regions; this fiscal externality is the principal source of the inefficiency. But the increase in tax base relative to the national average also reduces the deviating government’s entitlement under an equalization formula. This offsets the impact of the tax cut on own-source revenue, and so tends to increase equilibrium tax rates of all regions. In fact, in a central case, we are able to show that the equalization effect exactly offsets the fiscal externality, making regional governments willing to implement the tax policies that would be chosen by a unitary central government.

To make this point, we lay out a popular theory of local capital tax competition and consider the effects of equalization grants on Nash equilibrium tax rates.<sup>3</sup> In the canonical version of the model, capital is in fixed supply to the nation as a whole, but mobile among regions; thus Nash equilibrium tax rates lie below the level that would be chosen by a unitary central government.

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<sup>1</sup>Oates (1972) is probably the best-known elaboration of the trade-offs involved in allocation of taxing and spending powers to different levels of government.

<sup>2</sup>These include Canada, Denmark, Sweden, Switzerland, and a large number of developing countries. As well, the equalization formula is the basis of local school district finance in a number of US states (Card and Payne, 2002).

<sup>3</sup>The model is originally due to Wilson (1986) and Zodrow and Mieszkowski (1986). Here we consider an expanded version of the model that incorporates (elastic) savings behaviour, as in Keen and Kotsogiannis (2001).

In this environment, we show that an equalization grant induces regional governments to set tax rates efficiently, while simultaneously equalizing revenue among the regions. Thus equalization decentralizes a central government's preferred allocation.

Of course, many federal grant systems other than equalization could also be designed to achieve the optimum; all that must be done is to set the slope of the transfer formula to correct regional governments' incentives, and to set the intercept to equalize spending appropriately. Thus, for example, Wildasin (1991) proposes a system of linear matching grants for local tax rates, and Figuières, Hindriks and Myles (2001) a transfer system that pools a fraction of local revenues and shares it equally among all governments. What is noteworthy about our result is that a simple equalization formula decentralizes the optimum in a rich set of environments, regardless of the degree of regional mobility of capital, and regardless of a variety of differences in the tax capacities and populations of regions. The simplicity of the formula is an attractive feature of equalization, especially when differences among regions are large and variable over time—which seems to be precisely when such grants are most often observed in practice.

So far, our results deal with the case of a fixed national tax base that is mobile among regions. But taxes generally have distortionary effects at the national as well as regional level. We therefore consider an extended version of the model, in which capital is elastically supplied by consumers, and we show that full equalization leads to equilibrium tax rates higher than optimal. Even in this case, however, a simple fix is available: the optimum can be decentralized by a system of "partial" equalization that compensates regions for a proper fraction of differences in revenue capacity. The optimal fraction is equal to the fraction of coordinated national tax increases that is shifted backward to capital owners, a parameter that can be easily estimated. Moreover, the optimal formula is the same for all jurisdictions, regardless of differences in local tax capacity, tastes, or population.

Our results have important antecedents in the literature. Boadway and Flatters (1982) and Flatters et al. (1974) show that equalization transfers may be needed to eliminate fiscally induced migration that would reduce labour productivity.<sup>4</sup> Closer to our work, Smart (1998) shows how an equalization grant induces inefficiently high tax rates on a tax base that is elastically supplied but immobile among regions. The direction of the effect in this paper is the same but, because of regional mobility, the normative implications are quite different. The general notion that federal revenue sharing can align local government incentives and reduce tax competition is much older, and is discussed by Brennan and Buchanan (1980), among others. Boadway and Hayashi (2001) and Esteller-Moré and Solé-Ollé (2002) provide evidence that equalization has reduced business tax competition among provincial governments in Canada. Köthenbürger (2002) also establishes our basic result for the case of identical regions and fixed aggregate capital supply. Here we extend the analysis to elastic tax bases and show how the effects of equalization are robust to regional inequality and differences in tastes and population.

The plan of the paper is as follows. Section 2 presents the model, describes the Nash equilibrium, and characterizes transfer systems that implement the central government's optimum. Section 3 establishes our basic result for the simplest case, in which national aggregate tax bases are fixed, and regional productivity differences take a simple form. Section 4 extends the argument to elastic tax bases, to more general forms of regional inequality, and to regional population differences. Section 5 examines an extension of the model in which equalization may serve to correct a government commitment failure. Section 6 concludes the paper.

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<sup>4</sup>In contrast to our work, governments do not behave strategically in these papers.

## 2 A model of tax competition in a federation

A federal economy consists of  $N$  regions. In each region, firms produce a consumption good (the numeraire) with a linear-homogeneous technology, using an immobile factor, land, and a mobile factor, capital. Since the land input is fixed in each region, we suppress it from notation and write the aggregate production of region  $i$  as  $f_i(k_i)$ , if  $k_i$  units of capital are employed there. Capital is paid its marginal product, and the rents to land are the residual amount  $\pi_i(k_i) = f_i(k_i) - k_i f'_i(k_i)$ .

A population of  $n_i$  identical citizens resides in each region and is endowed with all of the local land input and  $B$  units of the consumption good. Agents consume at two dates, both before and after production takes place. Thus they elastically supply  $s_i$  units of the good for use as capital by firms, while consuming the balance  $c_i^1 = B - s_i$  in the first period. Capital moves freely among regions in the federation and is allocated to maximize returns to capitalists. Accordingly, in equilibrium, it earns an equal net rate of return  $r$  in each jurisdiction, and agents receive total factor incomes

$$c_i^2 = \pi_i(k_i) + (1 + r)s_i \quad (1)$$

which are available for consumption in the second period.<sup>5</sup> In the second period, citizens also consume a local public good  $g_i$ . Citizens in all jurisdictions have quasi-linear preferences over bundles of public and private consumption  $u(c_i^1) + c_i^2 + b_i(g_i)$ , where each  $b_i$  is a strictly concave function.

Let

$$v(k_i, r) = \max_s \{u(B - s) + c_i^2 : c_i^2 = \pi_i(k_i) + (1 + r)s\}$$

represent the indirect utility from private consumption of the representative agent in region  $i$ , and let  $s(r)$  be the associated utility-maximizing supply of capital. Observe that, because preferences are quasi-linear, optimal saving is independent of income and so is independent of domestic investment and land rents.

To finance spending on the local public good, each local government levies a specific, source-based tax  $t_i$  on capital employed in the jurisdiction. Firms in each jurisdiction choose investment to maximize profit, taking the gross cost of capital  $r + t_i$  as given; thus each region's capital demand function is defined by the usual marginal condition

$$k_i = \phi_i(r + t_i) \iff f'_i(k_i) = r + t_i \quad (2)$$

Observe that  $\phi'_i(r + t_i) = 1/f''_i(k_i) < 0$ .

Since taxes are levied on mobile capital, their burden may be borne in equilibrium by landowners within the region, or by capitalists throughout the federation. To describe the effects of taxes on market equilibrium, let  $S(r) = Ns(r)$  denote the aggregate supply function for capital in the federation. Given tax rates  $t = (t_1, \dots, t_N)$ , the capital market in this economy clears at an interest rate  $r^*(t)$  such that

$$\sum_i \phi_i(r^* + t_i) = S(r^*) \quad (3)$$

which in turn yields the equilibrium investment levels  $k_i^*(t) = \phi_i(r^*(t) + t_i)$ . Implicit differentiation then yields the comparative static derivatives

$$\frac{\partial r^*}{\partial t_i} = \frac{\phi'_i(r^* + t_i)}{S'(r^*) - \sum_j \phi'_j(r^* + t_j)} < 0 \quad (4)$$

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<sup>5</sup>Observe that there are by assumption no residence-based income taxes in the economy.

$$\frac{\partial k_i^*}{\partial t_i} = \phi_i'(r^* + t_i) \left( 1 + \frac{\partial r^*}{\partial t_i} \right) < 0 \quad (5)$$

and

$$\frac{\partial k_j^*}{\partial t_i} = \phi_j'(r^* + t_j) \frac{\partial r^*}{\partial t_i} > 0 \quad j \neq i \quad (6)$$

Thus a unilateral tax increase in jurisdiction  $i$  causes a decline in the equilibrium interest rate, and investment declines at home but rises elsewhere.

## 2.1 Nash equilibrium

Local governments behave non-cooperatively, using the source-based tax rates  $t_i$  as their strategic variables. They also respond to a transfer formula chosen by a central government. The timing of events is: first, the central government commits to a transfer formula  $T_i(t_1, t_2, \dots, t_N)$  defining the net transfer to each jurisdiction as a function of the tax rates; second the jurisdictions choose their tax rates  $t_i$  simultaneously; third, consumers and firms make their saving and investment decisions; fourth, production and consumption take place. The quantity of public goods provided in jurisdiction  $i$  is

$$g_i = t_i k_i^*(t) + T_i(t) \quad (7)$$

Each jurisdiction's government chooses its tax rate to maximize the utility of its citizens,  $v(k_i^*(t), r^*(t)) + b_i(g_i)$  subject to the budget constraint (7), taking as given the other jurisdictions' tax rates, and the central government's transfer formula. The first-order condition for this problem is

$$k_i^* + (k_i^* - s) \frac{\partial r^*}{\partial t_i} = b_i'(g_i) \left[ k_i^* + t_i \frac{\partial k_i^*}{\partial t_i} + \frac{\partial T_i}{\partial t_i} \right] \quad (8)$$

The left side of equation (8) is the marginal cost, in reduced consumption of the private good (in the second period), of a tax increase in the jurisdiction. The right side is the marginal benefit of the increase in public good consumption resulting from the tax increase.<sup>6</sup> Note that the transfer formula will tend to encourage tax effort if the size of the transfer received by the jurisdiction increases with the jurisdiction's tax rate.

## 2.2 Optimal taxes in a unitary state

As a benchmark, consider the optimum for a central government which could set each jurisdiction's tax rate directly, and which could allocate this tax revenue for public good provision in each jurisdiction. However the central government is not allowed to transfer income in a lump-sum fashion among jurisdictions. If each jurisdiction had the same population, and if the central government wished to maximize the sum of people's utilities in the federation, then it would choose the tax rates to maximize

$$\sum_i [v_i(k_i^*, r^*) + b_i(g_i)]$$

subject to the consolidated national budget constraint

$$\sum_i g_i = \sum_i t_i k_i^* \quad (9)$$

<sup>6</sup>The left side of the equation must be positive, since equation (4) shows that  $\partial r^* / \partial t_i$  must be less than 1 in absolute value. Therefore, if  $t_i$  is a best response for jurisdiction  $i$ , then the right side must be positive as well.

The unitary optimum is therefore described by the first-order conditions

$$b'_i(g_i) = \mu \quad (10)$$

and

$$k_i = \mu \left( k_i + \sum_j t_j \frac{\partial k_j^*}{\partial t_i} \right) \quad (11)$$

where  $\mu$  is the Lagrange multiplier on the consolidated government budget constraint (9).

The first condition implies that the marginal benefit of the public good is equalized in all jurisdictions; when preferences for the public good are identical among regions, this implies uniform provision as well. The second condition (11) implies equalization of the marginal deadweight loss of each region's source-based tax  $t_i$ ; in particular, each regional government must internalize the (positive) effect of tax increases on revenues in other jurisdictions.

Comparing (11) and (8) gives a decomposition of the externalities that each jurisdiction's tax policy imposes on the others: if an intergovernmental transfer system  $T^*$  decentralizes the centralized optimum allocation, then

$$\frac{\partial T_i^*}{\partial t_i} = \sum_{j \neq i} t_j^* \frac{\partial k_j^*}{\partial t_i} + \frac{1}{b'_i(g)} \frac{\partial r^*}{\partial t_i} (k_i - s) \quad (12)$$

This transfer system implements a marginal subsidy to local tax collections that has a Pigouvian interpretation. The first term in (12) is the external effect of a tax increase in  $i$  on revenues collected in other jurisdictions  $j \neq i$ , identified in Wildasin (1989). The second term, discussed in DePater and Myers (1994), is the "terms of trade" effect of a tax increase on net capital income in region  $i$ ; this effect is positive for a net capital importer and negative for a net exporter. Since exports from one jurisdiction equal imports by all others, the marginal terms of trade gain to the home jurisdiction equals the marginal damage imposed on the others, and the Pigouvian subsidy offsets this pecuniary external effect as well.

### 2.3 Equalization grants

Equalization grants represent a particular form of transfer. In its idealized form, an equalization grant system would ensure that each jurisdiction would provide the average level of public goods for the federation, were the jurisdiction to levy the national average tax rate. This system, which we will call "full equalization," therefore implies a transfer of

$$T_i^E = \bar{t}(\bar{k} - k_i) \quad (13)$$

where the national average tax rate is

$$\bar{t} \equiv \frac{\sum_j t_j k_j}{\sum_j k_j}$$

and the national average tax base is

$$\bar{k} \equiv \frac{\sum_j k_j}{N}$$

If  $R \equiv \sum t_j k_j$  denotes the total tax revenue in the federation, and  $K \equiv \sum k_j$  the total capital demand in the federation, then equation (13) can be written

$$T_i^E = R \left( \frac{1}{N} - \frac{k_i}{K} \right) \quad (14)$$

Thus equalization pays each jurisdiction a fraction of national revenues equal to the difference between its population share and its share of the tax base. In what follows, we will also consider a system of *partial equalization*, in which a fraction  $\alpha$  of differences in local revenue capacity are equalized, so that  $T_i = \alpha T_i^E$ .

To understand how equalization affects each government's incentives in setting taxes, it is useful to consider the marginal change in transfers resulting from a local tax increase. Differentiation of equation (14) yields

$$\frac{\partial T_i^E}{\partial t_i} = \left( \frac{1}{N} - \frac{k_i}{K} \right) \frac{\partial R}{\partial t_i} - \frac{R}{K} \left( \frac{\partial k_i^*}{\partial t_i} - \frac{k_i}{K} \frac{\partial K}{\partial t_i} \right) \quad (15)$$

Comparing the marginal incentives under equalization to the optimal grant system (12) is our focus in most of what follows.

### 3 Efficient equalization: An example

Inspection of the marginal equalization grant in (15) leaves the effects of the transfer far from clear and, comparing the optimal grant in (12), there appears no reason to expect that equalization can decentralize optimal local taxes. To show why this is so, it may be helpful to first consider a simpler case, with fixed saving, and similar tastes and technologies in all regions. In particular, we assume:<sup>7</sup>

**Assumption 1:** Capital supply is  $s(r) = \bar{s}$ , independent of the interest rate  $r$ ; and

**Assumption 2:** Capital demand functions are  $\phi_i(\rho) = \phi(\rho)$ , identical in all regions.

**Assumption 3:** Preferences for the public good are  $b_i(g) = b(g)$ , identical in all regions.

We will relax these assumptions in Section 4 below.

Assumption 1 is sufficient to guarantee that the optimal tax system is uniform across jurisdictions, so that the allocation of capital achieves production efficiency.<sup>8</sup> Thus we have:

**Lemma 1** *Under Assumption 1, the unique unitary optimum involves equal taxation of capital in all jurisdictions at the rate*

$$t^* \equiv \sum g_i^* / (N\bar{s})$$

where

$$g_i^* = b_i'^{-1}(1) \quad (\text{all } i)$$

<sup>7</sup>This is the environment considered by Köthenbürger (2002).

<sup>8</sup>The unitary optimum does not generally involve production efficiency, however: a national government may prefer to distort the allocation of capital among regions in order to redistribute consumption among local residents. We return to this point below.

*Proof.* See the appendix.<sup>9</sup>

Can this optimum be implemented by an equalization grant? The answer is yes. Since Lemma 1 implies optimal taxes are uniform, and since technologies are identical, the equilibrium capital allocation is symmetric:  $k_i = \bar{s}$  for all  $i$ . The marginal equalization grant in (15) then simplifies to

$$\frac{\partial T_i^E}{\partial t_i} = -t^* \frac{\partial k_i^*}{\partial t_i}$$

Faced with an equalization grant, each jurisdiction sets its tax rate to satisfy the first-order condition (8), which simplifies to

$$k_i = b'(g_i)k_i \quad (16)$$

Moreover, symmetry implies  $g_i = t^*\bar{s}$  for each jurisdiction; thus (16) coincides with the first-order condition (12) describing the unitary optimum tax rate. Therefore, full equalization yields a Nash equilibrium to the tax-setting game played by the jurisdictions, in which they all choose the optimal tax rates, and spend the optimal amount on the public good.

In this case, since the equilibrium is symmetric, no transfers are actually paid in equilibrium. Nevertheless, a deviation by any regional government from the optimal tax rate would induce a change in transfers that exactly offsets the “base” effect of the tax change  $t^*\partial k_i^*/\partial t_i$ . Thus each government optimally behaves as though its tax base were independent of the local tax rate; since the national base is indeed perfectly inelastic, this induces optimal tax policies.

In reality, equalization grants are typically paid when there are substantial differences in local tax capacities; it is regional inequality, rather than tax competition, that principally motivates the transfers. It therefore seems important to incorporate regional inequality into the analysis. To this end, we replace Assumption 2 by:

**Assumption 2’:** Capital demands have the form  $\phi_i(\rho) = A_i\phi(\rho)$  for some parameters  $A_i$  such that  $\sum_i A_i = N$ .

Thus the productivity of capital in any two regions may differ, but only by a constant percentage amount at any level of investment. This guarantees that the elasticity of tax bases is the same in all regions, even though the level of tax bases may differ. The following result shows that equalization decentralizes the optimal tax system in this case, regardless of the distribution of regional productivity levels  $A_i$ .

**Proposition 1** *Under Assumptions 1, 2’, and 3, a system of full equalization implements the unitary optimum tax system.*

*Proof.* Since saving is inelastic, the unitary optimal policy sets  $\mu = b'(g_i) = 1$  for all  $i$ . Since optimal taxes are uniform, (12) implies a transfer formula will implement the optimum only if

$$\frac{\partial T_i^*}{\partial t_i} = -t^* \frac{\partial k_i^*}{\partial t_i} + \frac{\partial r^*}{\partial t_i}(k_i - s)$$

whereas the marginal equalization grant is

$$\frac{\partial T_i^E}{\partial t_i} = -t^* \frac{\partial k_i^*}{\partial t_i} - \frac{1}{K} \frac{\partial R}{\partial t_i}(k_i - s)$$

<sup>9</sup>It should be clear that the policy described in the lemma satisfies the first-order conditions (10)–(11) for optimality; the proof also shows that this is an optimal policy, and that it is the only optimal policy.

But, since saving is inelastic,  $\partial R/\partial t_i = k_i$ , and (4) implies

$$\frac{\partial r^*}{\partial t_i} = -\frac{A_i}{N} = -\frac{k_i}{K}$$

where the last equality uses the multiplicative form of productivity differences of Assumption 2'. Finally, observe that when tax rates are uniform transfers equalize government spending in all jurisdictions to  $g_i = t^*K/N$ . Thus equalization decentralizes the unitary optimal policies.  $\square$

Observe that the equalization grant exerts two effects on behaviour in Proposition 1. First, it causes local governments to account for the externality their decisions about tax rates impose on the revenues accruing to other governments. But the problem in this environment is more complex: in addition to the fiscal externality, local tax policies are distorted by the pecuniary externality among regions. Because local tax cuts exert some positive effect on the rate of return to capital in the nation, low-productivity, capital exporting regions prefer lower capital taxes than do high-productivity, capital importing regions. This effect is independent of the direct effect of tax cuts on local tax bases and on government revenues. Nevertheless, the proposition shows that an equalization grant causes regional governments to internalize the pecuniary externality as well.

Of course, any grant system which achieved the appropriate ‘‘Pigouvian’’ marginal subsidy to local tax collections, as described by (12), and which equalized the marginal benefit of the public good in all regions, would decentralize the unitary optimum. Thus an equalization grant does not *uniquely* implement the optimum. For example, Figuières, Hindriks and Myles (2001) show how the optimum can be achieved through a grant system which pooled a particular fraction of local tax revenues and redistributed it on an equal per capita basis.<sup>10</sup> But decentralization through revenue pooling requires the federal government to observe the elasticity of local tax base function  $\phi$  and to set the share of revenues to be pooled appropriately; equalization achieves the optimum more parsimoniously. When regional tax bases are unequal, moreover, an optimal system of revenue pooling would require the grant formula to be differentiated among regions, whereas equalization is robust to regional inequality.

In the model presented here, it has been assumed that tax rates are the strategic variables in the non-cooperative game played by regional governments. It is known that the Nash equilibrium allocation is in general sensitive to whether regional governments conjecture that other regions are holding tax rates constant, or holding the level  $g_j$  of public expenditure constant, or some combination of the two. Figuières, Hindriks and Myles (2001) have shown that the appropriate central government remedy will differ in each of these cases as well. However, a virtue of the equalization formula  $T_i^E$  is that, when regions are identical and saving is fixed, its efficiency does not depend on the choice of strategic variable by the regions. This invariance is the consequence of the fact that marginal changes in one region’s tax rate have no effect at all on the budget constraint faced by any other region. To see this, differentiate the regional budget constraint (7) to obtain

$$\frac{\partial g_i}{\partial t_j} = t_i \frac{\partial k_i^*}{\partial t_j} + \bar{t} \left[ \frac{\partial \bar{k}}{\partial t_j} - \frac{\partial k_i}{\partial t_j} \right] + \frac{\partial \bar{t}}{\partial t_j} \left[ \bar{k} - k_i^* \right] = \bar{t} \frac{\partial \bar{k}}{\partial t_j} \quad (17)$$

since  $t_i = \bar{t}$  and  $\bar{k} = k_i^*$  at the optimum, if regions are identical. Thus fiscal spillovers are absent under full equalization, if  $\bar{k}$  is fixed. Because marginal changes in region  $j$ ’s tax rate do not affect any other region’s budget constraint, region  $j$ ’s conjectures about the other regions’ behaviour do

<sup>10</sup>They consider fiscal competition for mobile workers rather than capital, but the model is formally equivalent.

not matter: whatever the conjecture, deviations by region  $j$  would have no effect on the levels of the strategic variables chosen by the other regions.

Furthermore, equalization decentralizes the unitary optimum even in cases where the central government lacks sufficient information to impose optimal taxes directly. In the environment of Proposition 1, suppose that willingness to pay for the public good  $b(g_i)$  were common to all regions and observed by regional but not federal authorities.<sup>11</sup> Since the optimal tax rate satisfies  $b'(t^*K/N) = 1$ , achieving the optimum requires local information. Since the marginal subsidy provided by the equalization grant is scaled automatically by the average tax rate of all jurisdictions, an equalization grant is an indirect mechanism achieving (Bayesian) implementation of the unitary optimum.

## 4 Partial equalization: The variable saving case

### 4.1 The main result

The example of Section 3 show that, when the national tax base is perfectly inelastic, an equalization grant decentralizes the optimum by compensating regional governments for increasing tax rates in such a way that they behave as if their own tax bases were inelastic, despite regional mobility of capital. But even coordinated national increases in capital tax rates have distortionary effects, when saving is elastically supplied. Can equalization provide the right incentives for regional governments in this environment?

Without Assumption 1, characterizing optimal policies is more complicated, and tax rates need not be uniform in general. Manipulating the first-order conditions (11) for the planner's problem gives the following "inverse elasticity" expression for optimal tax rates.

**Lemma 2** *At the utilitarian optimum allocation, if  $s'(r^*) > 0$ , local tax rates satisfy*

$$t_i^* = \frac{\mu - 1}{\mu} \left( \frac{s(r^*)}{s'(r^*)} - \frac{\phi_i(r^* + t_i^*)}{\phi_i'(r^* + t_i^*)} \right) \quad (18)$$

where  $\mu = b_i'(g_i^*)$  for all  $i$ .

*Proof.* See the appendix.

Under Assumption 2', it is immediate from (18) that a uniform tax system again satisfies the first-order conditions. Under an additional condition, it can be shown that uniformity is in fact necessary for an optimum: Suppose that the capital demand function  $\phi$  is log-concave (i.e.  $\phi'/\phi$  is a non-increasing function).<sup>12</sup> Then

$$-\frac{\phi(r + t_i)}{\phi'(r + t_i)} \leq -\frac{\phi(r + t_j)}{\phi'(r + t_j)}$$

whenever  $t_i \geq t_j$ . It follows that  $t_i^* = t_j^*$  at any solution to (18).<sup>13</sup>

<sup>11</sup>See Bucovetsky, Marchand and Pestieau (1998) for a full model along these lines.

<sup>12</sup>This condition will hold if the Hicks–Allen elasticity of substitution  $\sigma$  between capital and land in production (defined so as to have a positive sign) is a non-decreasing function of the cost of capital  $\rho$ , and if  $\sigma$  is everywhere less than or equal to 1.

<sup>13</sup>If  $\phi$  were not log-concave, then there would still exist a solution to the central government's first-order conditions involving equal tax rates. However, there would be no guarantee that every solution to those conditions must have equal tax rates.

When saving is elastically supplied, full equalization tends to “oversubsidize” local tax increases and hence to result in equilibrium tax rates higher than optimum levels. To see this, consider again the case of identical regions. At any uniform tax system, the marginal equalization grant in (15) is

$$\frac{\partial T_i^E}{\partial t_i} = -t \left( \frac{\partial k_i^*}{\partial t_i} - \frac{1}{N} \frac{\partial K}{\partial t_i} \right)$$

so that equilibrium tax rates satisfy

$$\frac{1 - b'(g)}{b'(g)} K = t \frac{\partial K}{\partial t_i}$$

whereas the optimum requires

$$\frac{1 - b'(g)}{b'(g)} K = N t^* \frac{\partial K}{\partial t_i}$$

Since  $K$  is decreasing in  $t_i$ , equilibrium tax rates must exceed optimal levels. This echoes the results in Smart (1998).

Nevertheless, a simple régime of partial equalization can decentralize the optimum in this more general case, where the fraction of revenues to be equalized depends (only) on the semi-elasticities of capital demand and supply, viz.

$$e_d = - \frac{\phi'(r+t)}{\phi(r+t)}$$

$$e_s = \frac{s'(r)}{s(r)}$$

(Note that by convention these are measured as non-negative numbers.)

**Proposition 2** *Under Assumption 2', the unitary optimum can be decentralized by a system of partial equalization grants  $T_i = \alpha^* T_i^E$ , in which a fraction*

$$\alpha^* \equiv \frac{e_d}{e_d + e_s}$$

*of capacity differences are equalized, together with a system of lump-sum grants*

$$T_i^0 = g_i^* - \alpha^* T_i^E(t^*)$$

*Proof.* See the appendix.

To interpret the result, note that the expression for  $\alpha^*$  is equal to

$$\sum_i \frac{\partial r^*}{\partial t_i}$$

which is the fraction of coordinated national tax increases that are shifted backward to capital owners in equilibrium. The greater the degree of backward tax incidence, the less distortionary is the tax, and the higher the optimal rate of partial equalization. A particular implication of Proposition 2 is that, when capital is in perfectly elastic supply to the nation (the small open economy case), equalization grants should not be paid.

## 4.2 General technologies – and many regions

Suppose now that regional productivity differences do not take the particular multiplicative form of Assumption 2'. It need not be true that each region should levy the same tax rate, and it need not be true that the equalization formula must be uniform, at the rate  $\alpha^*$ .

Equation (18) still characterizes the utilitarian optimum. The question addressed in this section is what form of equalization grant will implement the optimal tax rule (18) in this general case.

It will be assumed here that there are a fixed number  $M$  of production functions, where the number  $M$  may be arbitrarily large, but is finite. Each of the  $N$  regions has a production function drawn from this set of  $M$  possible functions. Each of the regions has the same population, 1, and the same endowment  $B$  of the consumption good. In this section, "small" regions will be considered, by increasing the number  $N$  of regions. (The number  $M$  of possible technologies will be held fixed, just as the number of types of consumer is held constant when the number of consumers is increased, as in much of the literature on core equivalence in large exchange economies.)

The optimal transfer system must satisfy condition (12), as before. However, as the number of regions grows large,  $\partial r^* / \partial t_i$  approaches zero in (4), and the second term vanishes from the optimal equalization formula: Since small regions cannot affect the terms of trade for capital imports, a utilitarian central government need not correct for the pecuniary externality. On the other hand, the fiscal externality is bounded above zero and, for any  $N$ , is equal to

$$\frac{\phi'_i}{Ns' - \sum_j \phi'_j} \sum_{j \neq i} t_j^* \phi'_j \quad (19)$$

Now, let

$$\bar{t} = \lim_{N \rightarrow \infty} \frac{\sum_j t_j^* \phi'_j}{\sum_j \phi'_j}$$

which is an average of the regions' tax rates, weighted now not by capital demands, but by their derivatives  $\phi'_j$ , and let

$$\alpha^* = \lim_{N \rightarrow \infty} \frac{-\sum_j \phi'_j / N}{s' - \sum_j \phi'_j / N} \equiv \frac{\bar{e}_d}{e_s + \bar{e}_d}$$

where  $\bar{e}_d$  is here defined as (minus) the semi-elasticity of *aggregate* capital demand  $\sum \phi_j$ . Rearranging in (19) and taking limits then gives

$$\frac{\partial T_i^*}{\partial t_i} \rightarrow -\alpha^* \bar{t} \phi'_i (r^* + t_i^*) \quad \text{as } N \rightarrow \infty \quad (20)$$

What of incentives for small regions under an equalization grant  $T_i^E = \bar{t}(\bar{k} - k_i)$ ? Analogous arguments show that the marginal effect of  $t_i$  on the average tax rate  $\bar{t}$  and average tax base  $\bar{k}$  vanish as  $N$  grows large. Hence, in the limit,

$$\frac{\partial T_i^E}{\partial t_i} \rightarrow \bar{t} \phi'_i (r + t_i) \quad (21)$$

Comparison of equations (20) and (21) then gives the limiting result:

**Proposition 3** *As the number of regions  $N$  grows large, the formula which implements the utilitarian optimum approaches partial equalization of tax bases at the same rate in all regions, with that rate equal to  $\alpha^* \bar{t} / \bar{t}$ .*

When regional inequalities in productivity take an arbitrary form, and capital is elastically supplied, then the central planner typically prefers regional governments to levy non-uniform tax rates. Nevertheless, the optimum can be decentralized, at least asymptotically, by a uniform system of equalization grants. The fraction of revenues to be equalized is however smaller than in the case of uniform taxes. From the central planner's optimality condition (18), regions with low tax rates have high absolute values of  $\phi'_j / \phi_j$ , so that

$$\bar{t} = \frac{\sum t_j^* \phi'_j}{\sum \phi'_j} \leq \frac{\sum t_j^* \phi_j}{\sum \phi_j} = \bar{t}$$

In this sense, greater inequality among regions undermines the case for tax base equalization.

### 4.3 Regional population differences

When regions differ in productivity, Proposition 2 shows that the equalization formula must be supplemented by lump-sum grants, which vary with a jurisdiction's characteristics. However, there is one case in which partial equalization alone is sufficient, even when jurisdictions differ in at least one respect. Suppose that each jurisdiction has the same tastes and technology, but that the jurisdictions have different populations. In this case, not only is the Nash equilibrium inefficient in the absence of transfers, it also involves tax rates differing among jurisdictions.<sup>14</sup> In this case, then, there are some inequalities for transfers to equalize.

Modifying slightly the notation of the previous sections, let  $k_i$  and  $g_i$  denote the *per capita* capital stock and public goods consumption in jurisdiction  $i$ . We normalize regional populations so that each  $n_i$  denotes the population in  $i$  relative to the average region; hence  $\sum n_i = N$ . We again assume identical tastes for the public good in each region. The utilitarian optimum is now  $\sum_i n_i [v_i(k_i^*, r^*) + b(g_i)]$ . Maximizing this subject to the aggregate budget constraint  $\sum_i n_i (t_i k_i^* - g_i) = 0$  leads to the first-order conditions (10) and

$$n_i k_i = \mu \left[ n_i k_i + \sum_j n_j t_j \frac{\partial k_j^*}{\partial t_i} \right] \quad (22)$$

Now the effect of a jurisdiction's tax rate on the net rate of return, obtained from differentiation of the aggregate capital market clearing condition  $S(r^*) = \sum_i n_i \phi_i(r^* + t_i)$  is<sup>15</sup>

$$\frac{\partial r^*}{\partial t_i} = \frac{n_i \phi'_i(r^* + t_i)}{S'(r^*) - \sum_j n_j \phi'_j(r^* + t_j)} \quad (23)$$

In this more general environment, Lemma 2 continues to hold: in particular, the optimal tax system is uniform among jurisdictions when technologies are everywhere identical. But, if there were no transfers among jurisdictions, then tax rates could not be equal in any Nash equilibrium: If  $t_i = t_j$  and if  $n_i > n_j$  then (using (6) and (23)) the right-hand side of the optimality condition (8)

<sup>14</sup>See Wilson (1991), or Bucovetsky (1991).

<sup>15</sup>The expressions for the effect of a tax change on the equilibrium capital allocation defined in (5) and (6) continue to hold, with  $\partial r^* / \partial t_i$  defined by equation (23) instead of (4).

would be greater for the larger jurisdiction, while the left-hand sides of the equation would be the same. Thus larger jurisdictions levy higher taxes in a Nash equilibrium without transfers, since they internalize more of the effects of tax increases than do small regions.

The formulae for equalization rules must also be modified slightly: Let  $K = \sum_i n_i k_i$  denote the national total (not per capita) tax base. Equation (13) defines each government's per capita entitlement, where the national weighted-average tax rate is now  $\bar{t} = \sum_i n_i t_i k_i / K$  and the per capita tax base is  $\bar{k} = K / N$ . Similarly, the revenue-sharing representation of the formula (14) holds where  $R = \sum_i n_i t_i k_i^*$  is national total revenue. With these definitions, the expression (15) for the marginal equalization grant continues to hold. We then have the following result.

**Proposition 4** *If jurisdictions differ in population, but not in tastes or technologies, then the utilitarian optimum can be implemented by a system of partial equalization grants at the rate*

$$\alpha^* \equiv \frac{e_d}{e_d + e_s}$$

Furthermore, no additional lump-sum transfers are required to achieve the optimum.

*Proof.* From Lemma 2, the tax rates in all jurisdictions should be equal at the optimum. When tax rates are equal, equation (22) becomes

$$k_i = \mu \left[ k_i + \frac{t}{n_i} \sum_j n_j \frac{\partial k_j^*}{\partial t_i} \right] = \mu \left[ k_i + t \frac{\phi' s'}{s' - \phi'} \right] \quad (24)$$

Also, when tax rates are equal,

$$\frac{\partial T_i^E}{\partial t_i} = -t \phi' \frac{N - n_i}{N} \quad (25)$$

so that

$$t \frac{\partial k_i^*}{\partial t_i} + \alpha \frac{\partial T_i^E}{\partial t_i} = t \frac{s' \phi'}{s' - \phi'} \quad (26)$$

Under partial equalization at the rate  $\alpha^*$ , the Nash equilibrium has each jurisdiction choosing a tax rate such that equation (8) holds, with  $T_i = \alpha^* T_i^E$ . From equation (26), that means

$$k_i = b'(g_i) \left[ k_i + t \frac{s' \phi'}{s' - \phi'} \right]$$

when all tax rates are equal, so that the Nash equilibrium satisfies the optimality condition (24) under partial equalization at the rate  $\alpha^*$ . Since this equilibrium has each jurisdiction levy the same tax rate, therefore all jurisdictions have the same tax revenue per person, and thus the same level  $g_i^*$  of public good provision per person. Equalizing all tax revenue at the rate  $\alpha^*$  leads to a Nash equilibrium in which every jurisdiction levies the same tax rate, and where the tax revenue in each jurisdiction is the efficient  $g_i^*$ , whatever is the population distribution, thus proving the proposition.  $\square$

## 5 Decentralization as a commitment device

In most of the cases studied in this paper, there is no informational advantage to decentralization: a federal government with sufficient information to design optimal transfers could simply

implement the optimal (though possibly non-uniform) tax rates directly through a unitary system of government. Thus the case for decentralization must rest on other grounds. One motivation frequently pointed to in the literature is the “market-preserving” role of federalism (Qian and Weingast, 1997; Kehoe, 1989): in the presence of a variety of political failures, inter-jurisdictional competition places constraints on the powers of government that may be desirable. Of course, unfettered competition among governments is unlikely to be optimal in such circumstances; here we argue that equalization grants will also be required.

To make this point, we consider a problem of commitment failure in capital taxation.<sup>16</sup> The setup of the model is the same as in Section 4, but with identical technologies for simplicity, and with a change in the order of moves. Now, tax rates are chosen after investors have made their savings decision; investments are irreversible but are freely mobile among regions of the federation after tax rates have been announced.

With this timing, governments perceive the elasticity of capital supply to be zero when tax rates are chosen. Lemma 1 shows that a central government with powers of taxation would impose a uniform tax in all regions at the rate  $t = b'^{-1}(1)/s$ . Comparing the full commitment optimal tax (18) shows that taxes would be too high and, in equilibrium, savings would be too low.

Now suppose that the central government can commit to transfer its tax powers to the regions, and to an equalization formula, prior to investments being sunk. From the perspective of regional governments, the aggregate supply of capital will still be fixed but mobile among regions. Tax competition among regional governments will therefore obviate the commitment problem in taxation, but equilibrium tax rates will generally differ from the full-commitment optimum. However, we can show:

**Proposition 5** *Suppose that, prior to investments being sunk, the central government transfers tax powers to the regional governments and implements a system of partial equalization at rate*

$$\alpha' = 1 - \frac{N}{N-1} \frac{e_s}{e_s + e_d} \quad (27)$$

*Then the Nash equilibrium allocation coincides with the unitary optimal allocation under full commitment.*

*Proof.* Using (5), the perceived elasticity of each region’s tax base at any symmetric tax vector is

$$\frac{\partial k_i^*}{\partial t_i} = \frac{N-1}{N} \phi'$$

Likewise, the marginal equalization transfer is

$$\frac{\partial T_i^E}{\partial t_i} = t \frac{\partial k_i^*}{\partial t_i}$$

Suppose therefore that the federal government had committed to equalize some fraction  $\alpha$  of tax base differences. The first-order conditions (8) describing Nash equilibrium tax rates become

$$k_i = b'(g) \left( k_i + (1 - \alpha) t \frac{N-1}{N} \phi' \right)$$

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<sup>16</sup>We thank Torsten Persson for suggesting this approach.

The first-order conditions (13) characterizing optimal tax rates under full commitment are unchanged, but under our symmetry assumptions they simplify to

$$k_i = b' \left( k_i + t \frac{s' \phi'}{s' - \phi'} \right)$$

The two expressions are equivalent when (27) holds.  $\square$

As the number of regions  $N$  grows large, the optimal equalization rate approaches that of the full commitment case,  $\alpha^*$ . For finite  $N$ , however, the federal government should equalize a smaller fraction of capacity differences, in order to counteract the tendency of regional governments to perceive tax base elasticities as smaller than they actually are. In fact, the optimal fraction in (27) is negative whenever

$$e_s > (N - 1)e_d$$

In such cases, the true elasticity of capital supply is so large that even unfettered tax competition among the regions is insufficient to bring tax rates down to the optimal level. What is then required is a system that rewards governments with above-average tax bases and so enhances incentives to cut taxes. As  $e_s \rightarrow \infty$  (the case of a small open economy),  $\alpha'$  approaches its lower bound  $-1/(N - 1)$ .

## 6 Conclusion

Intergovernmental transfer systems are most often designed to increase equality of fiscal opportunities among regions. Typically, in economic models, equity objectives such as this are achieved only at some cost in economic efficiency; but in the case of intergovernmental grants that conclusion may well be reversed. When tax bases are mobile among regions, local tax effort creates a positive fiscal externality for others, and so tax effort is undersupplied in equilibrium. In this context, our analysis shows that a particular simple and commonly used system of tax base equalization grants creates an incentive for local governments to enhance tax effort, to the benefit of all in the nation. Indeed, if tax bases are regionally mobile but fixed in the aggregate, an equalization grant induces efficient behaviour by all local governments, without recourse to dictates from a central government about what tax policies should be adopted locally.

While the simplicity of this result is striking, the general conclusion is as expected. There will always be some grant formula (and in fact there will be many) that decentralize the unitary optimum policies. More remarkable is that our result continues to hold (at least when the tax base elasticity is the same in all regions) regardless of the pattern of regional inequality and of population among regions, and regardless of nation-wide shocks to the demand for public goods and to the elasticity of capital demand. This reflects two features of an equalization grant based on the representative tax system. First, because transfers are proportional to the average of local tax rates, the incentives embodied in the system scale naturally to the magnitude of fiscal externalities, even as the size of government desired by citizens changes. Second, the marginal subsidy to local taxes provided by equalization is larger when a local jurisdiction's tax base deficiency is larger. Thus an equalization also naturally counters the *pecuniary* externality among regions that causes small and low-productivity regions to impose a lower tax rate than large and high-productivity ones. Again, in the model we consider, this offset is exact: an equalization grant precisely internalizes both the fiscal and pecuniary externalities facing all regions.

Equalization grants therefore decentralize optimal tax policies in a federation in a wide set of circumstances, while other grant formulas would not. This fact might explain the apparent

popularity of equalization grants throughout the world, compared to other redistributive transfer systems.

The results just described apply only in the case that the nation-wide tax base is unaffected by coordinated national tax increases. When taxes also have distortionary effects at the national level, our conclusions are modified. A system of partial equalization grants can then decentralize optimal taxes, where the fraction of base deficiencies to be equalized is the same for all regions and equal to the fraction of national tax increases that are shifted backward to factor suppliers. In this case, however, a standard tradeoff between equity and efficiency is restored: without supplementary lump-sum grants, an equalization system that provides efficient incentives would leave some tax base inequalities unaddressed, whereas a fully equalizing transfer system would induce excessive local taxation.

## Appendix

**Proof of Lemma 1.** Given that the aggregate capital stock  $K$  is fixed, and the concavity of the production functions  $f_i(k_i)$ , aggregate output  $\sum_j f_j(k_j)$  is maximized if and only if the tax rates are equal across all jurisdictions. So the central government can always improve upon any policy in which tax rates are not all equal; if  $t = (t_1, t_2, \dots, t_N)$  is any vector of tax rates, set

$$t'_1 = t'_2 = \dots = t'_N = (\sum_j t_j k_j^*(t)) / K$$

and the same tax revenue will be raised as with the tax vector  $t$ , so that the same vector of public good levels  $g_i$  can be financed. Since the tax vector  $t'$  leads to a higher total level of output than does  $t$ , it leads to a higher value of

$$\sum_j v(k_j^*, r) = \sum_j [f_j(k_j) - t_j k_j]$$

Therefore, all tax rates must be equal at any solution to the central government's optimization problem. When the tax rates are equal, then the first order conditions (10) and (11) become  $b'(g_i) = 1$  for all jurisdictions  $i$ , so that the unique solution is for each  $g_i$  to equal  $g_i^*$  and for each tax rate to equal  $K / (\sum_j g_j^*)$ .  $\square$

**Proof of Lemma 2.** The first-order condition (11) for each  $t_i$  can be written as

$$\frac{1-\mu}{\mu} k_i = t_i \phi'_i + \frac{\partial r^*}{\partial t_i} \sum_j t_j \phi'_j \quad (28)$$

where we have used the expressions (4)–(6) for the derivatives of the equilibrium investment levels. Summing these equations for all  $i$  and noting  $\sum_i k_i = S$  gives

$$\frac{1-\mu}{\mu} S = \left( 1 + \sum_i \frac{\partial r^*}{\partial t_i} \right) \sum_i t_i \phi'_i = \frac{S'}{S' - \sum_i \phi'_i} \sum_i t_i \phi'_i \quad (29)$$

so that, when  $S' > 0$ ,

$$\sum_i t_i \phi'_i = \frac{1-\mu}{\mu} \frac{S' - \sum_i \phi'_i}{S'} S \quad (30)$$

Substituting (30) into (28) and rearranging gives

$$t_i = \frac{\mu - 1}{\mu} \left( \frac{S}{S'} - \frac{\phi_i}{\phi'_i} \right) \quad (31)$$

as desired.  $\square$

**Proof of Proposition 2.** When productivity differences take the multiplicative form, Lemma 2 implies that optimal taxes are uniform. With uniform taxes, the marginal transfer (12) required to decentralize the optimum becomes

$$\frac{\partial T_i^*}{\partial t_i} = t \left( \frac{\partial K^*}{\partial t_i} - \frac{\partial k_i^*}{\partial t_i} \right) + \frac{K}{\mu} \left( \frac{k_i}{K} - \frac{1}{N} \right) \frac{\partial r^*}{\partial t_i} \quad (32)$$

whereas the marginal equalization transfer (15) is

$$\frac{\partial T_i^E}{\partial t_i} = t \left( \frac{k_i}{K} \frac{\partial K^*}{\partial t_i} - \frac{\partial k_i^*}{\partial t_i} \right) - \left( \frac{k_i}{K} - \frac{1}{N} \right) \frac{\partial R}{\partial t_i} \quad (33)$$

When production functions differ only by multiplicative constants, then (4) becomes

$$\frac{\partial r^*}{\partial t_i} = - \frac{A_i}{N} \frac{e_d}{e_s + e_d} \quad (34)$$

which implies

$$\frac{\partial r^*}{\partial t} \equiv \sum_j \frac{\partial r^*}{\partial t_j} = - \frac{e_d}{e_s + e_d}$$

and

$$\begin{aligned} \frac{k_i}{K} \frac{\partial K}{\partial t_i} - \frac{\partial k_i}{\partial t_i} &= \left( \frac{\partial K}{\partial t_i} - \frac{\partial k_i}{\partial t_i} \right) + \left( \frac{k_i}{K} - 1 \right) \frac{\partial K}{\partial t_i} \\ &= (N - A_i) \phi' \frac{\partial r^*}{\partial t_i} + (A_i - N) s' \frac{\partial r^*}{\partial t_i} \\ &= -(N - A_i) (s' - \phi') \frac{\partial r^*}{\partial t_i} \\ &= \frac{1}{\partial r^* / \partial t} \left( \frac{\partial K}{\partial t_i} - \frac{\partial k_i}{\partial t_i} \right) \end{aligned}$$

Further, the planner's first-order condition for  $t_i$  can be written

$$\frac{\partial R}{\partial t_i} = \frac{k_i}{\mu} = \frac{K}{\mu} \frac{\partial r^* / \partial t_i}{\partial r^* / \partial t}$$

Substituting the last two expressions into (32) gives

$$\frac{\partial T_i^*}{\partial t_i} = - \frac{1}{\partial r^* / \partial t} t^* \left( \frac{\partial K}{\partial t_i} - \frac{\partial k_i}{\partial t_i} \right) - \frac{1}{\partial r^* / \partial t} \frac{K}{\mu} \left( \frac{k_i}{K} - \frac{1}{N} \right) \frac{\partial r^*}{\partial t_i} \quad (35)$$

It follows from (32) and (35) that the marginal equalization grant is optimal if  $T_i = \alpha T_i^E$ , where

$$\alpha = - \frac{\partial r^*}{\partial t} = \frac{e_d}{e_s + e_d} \quad \square \quad (36)$$

## References

- Boadway, R. W. and F. R. Flatters, 1982, Efficiency and equalization payments in a federal system of government: A synthesis and extension of recent results, *Canadian Journal of Economics* 15, 613–633.
- Brennan, G. and J. Buchanan, 1980, *The Power to Tax* (Cambridge University Press, New York).
- Bucovetsky, S., 1991, Asymmetric tax competition, *Journal of Urban Economics* 30, 167–181.
- Bucovetsky, S., M. Marchand, and P. Pestieau, 1998, Tax competition and revelation of preferences for public expenditure, *Journal of Public Economics* 44, 367–390.
- Bucovetsky, S. and J. D. Wilson, 1991, Tax competition with two tax instruments, *Regional Science and Urban Economics* 21, 333–350.
- Card, D. and A. Payne, 2002, School finance reform, the distribution of school spending, and the distribution of student test scores, *Journal of Public Economics* 83, 49–82.
- DePater, J. A. and G. M. Myers, 1994, Strategic capital tax competition: A pecuniary externality and a corrective device, *Journal of Urban Economics* 36, 66–78.
- Esteller-Moré, A. and A. Solé-Ollé, 2002, An empirical analysis of vertical tax externalities: The case of personal income taxation in Canada, *International Tax and Public Finance* 9.
- Figuieres, C., J. Hindriks, and G. Myles, 2001, Revenue sharing versus expenditure sharing, mimeo, CORE.
- Flatters, F. R., J. V. Henderson, and P. M. Mieszkowski, 1974, Public goods, efficiency and regional fiscal equalization, *Journal of Public Economics* 3, 99–112.
- Hayashi, M. and R. Boadway, 2001, An empirical analysis of intergovernmental tax interaction: The case of business income taxes in Canada, *Canadian Journal of Economics* 34, 481–503.
- Keen, M. J. and C. Kotsogiannis, 2002, Does federalism lead to excessively high taxes?, *American Economic Review* 92, 363–370.
- Kehoe, P., 1989, Policy cooperation among benevolent governments may be undesirable, *Review of Economic Studies* 56, 289–296.
- Köthenbürger, M., 2002, Tax competition and fiscal equalization, *International Tax and Public Finance* 9.
- Oates, W. E., 1972, *Fiscal Federalism* (Harcourt, Brace & Jovanovich, New York).
- Qian, Y. and B. Weingast, 1997, Federalism as a commitment to preserving market incentives, *Journal of Economic Perspectives* 11, 83–92.
- Smart, M., 1998, Taxation and deadweight loss in a system of intergovernmental transfers, *Canadian Journal of Economics* 31, 189–206.
- Tiebout, C., 1956, A pure theory of local expenditure, *Journal of Political Economy* 44, 416–424.

- Wildasin, D. E., 1989, Interjurisdictional capital mobility: Fiscal externality and a corrective subsidy, *Journal of Urban Economics* 25, 193–212.
- Wildasin, D. E., 1991, Income redistribution in a common labor market, *American Economic Review* 81, 757–774.
- Wilson, J. D., 1986, A theory of interregional tax competition, *Journal of Urban Economics* 19, 296–315.
- Wilson, J. D., 1991, Tax competition with interregional differences in factor endowments, *Regional Science and Urban Economics* 21, 423–451.
- Wilson, J. D., 1999, Theories of tax competition, *National Tax Journal* 52, 269–304.
- Zodrow, G. R. and P. Mieszkowski, 1986, Pigou, Tiebout, property taxation, and the underprovision of local public goods, *Journal of Urban Economics* 19, 356–370.